

$$m_f = \sqrt{2} \left( \frac{\beta - 1}{4} \right)^{1/4}, \quad m_f \approx \sqrt{2} + \frac{1}{4}$$